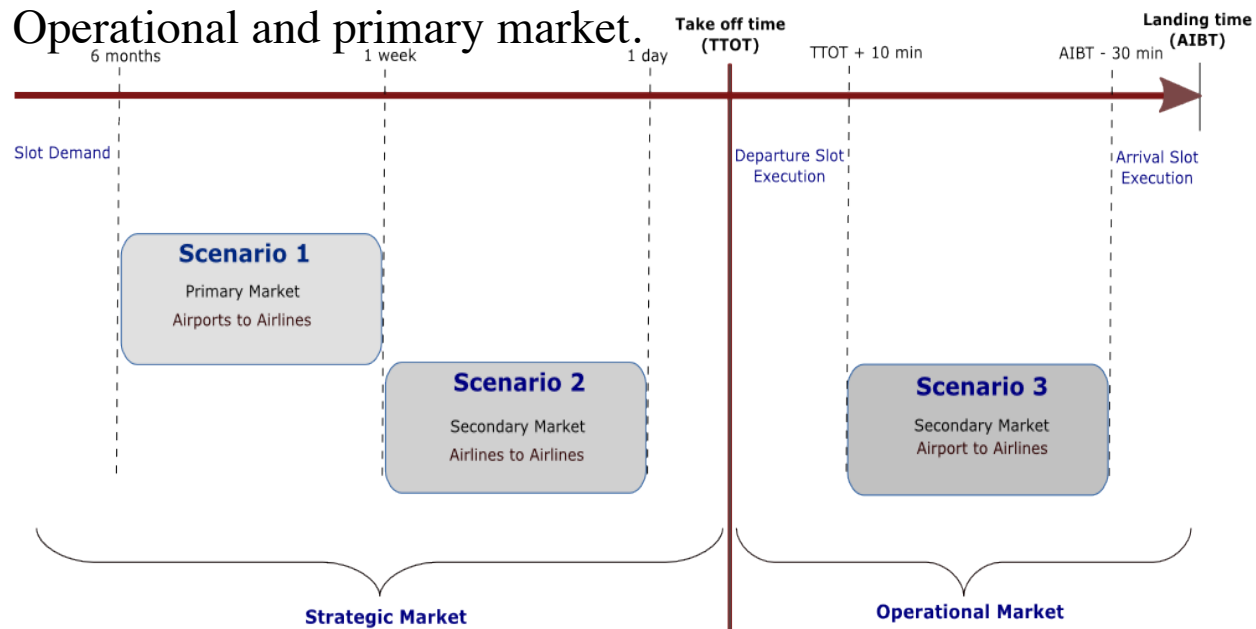


## SECURE MULTIPARTY COMPUTATION

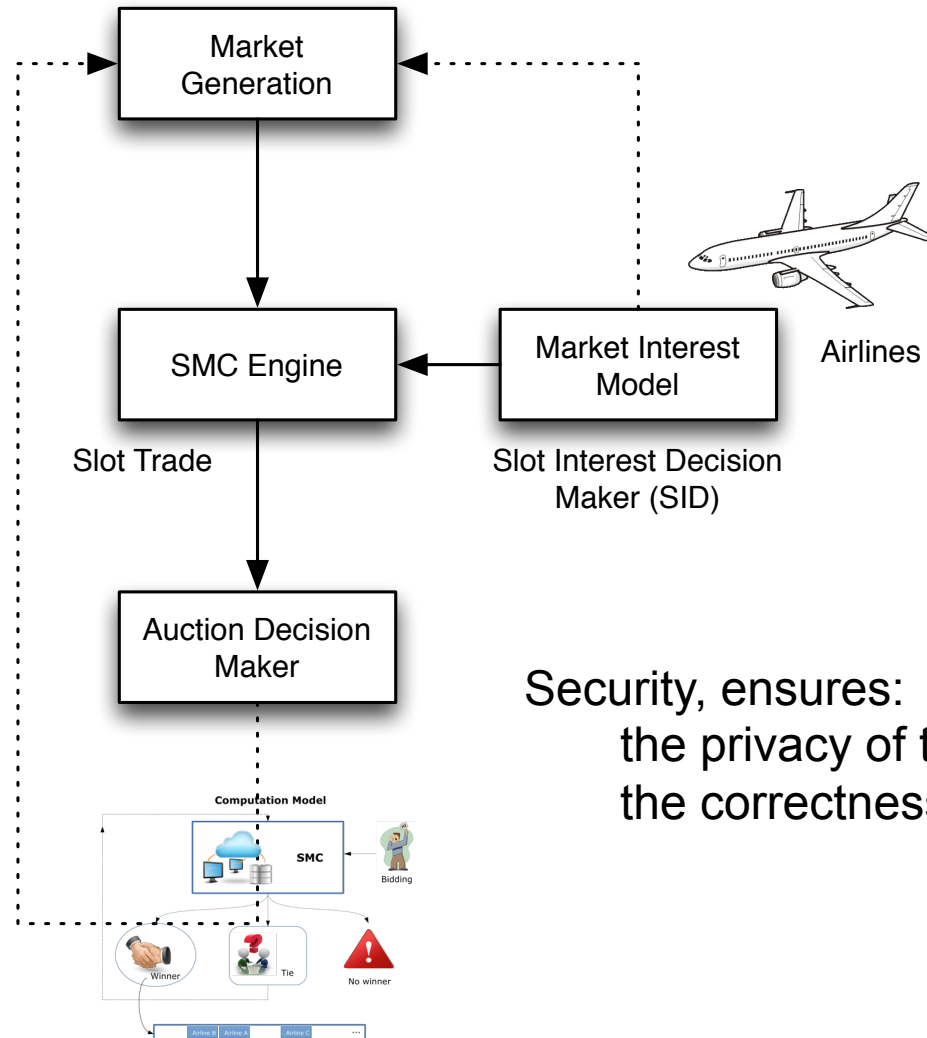
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**DR. EMRE KOYUNCU (ISTANBUL TECHNICAL UNIVERSITY)**

- Case scenarios:
  - **Scenario 1:** N airlines try to buy slots from an airport.  
Strategic and primary market.
  - **Scenario 2:** N airlines try to buy slots from another airline.  
Strategic and secondary market.
  - **Scenario 3:** N airlines try to buy a priority approach from an airport.  
Operational and primary market.



- General architecture

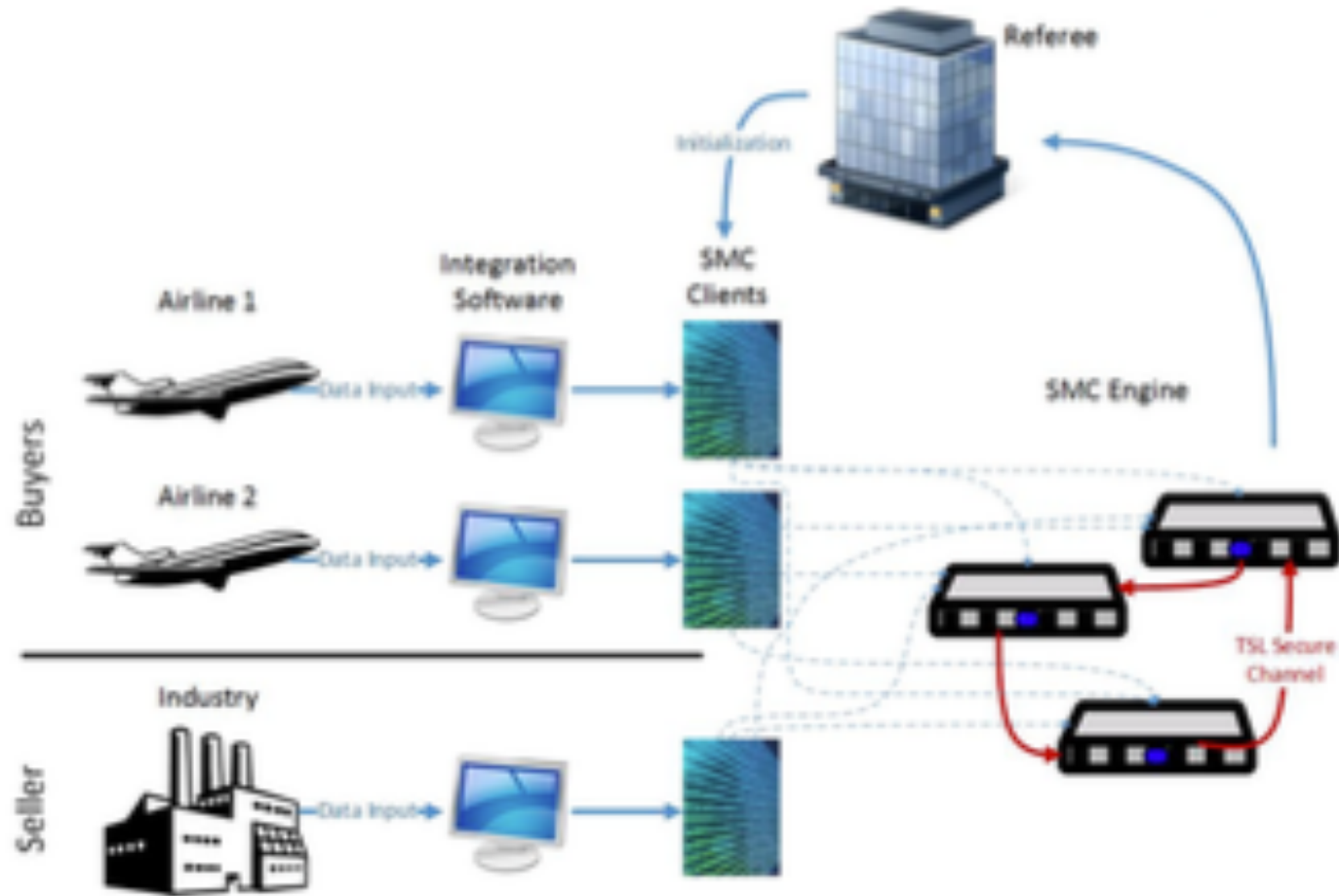


Security, ensures:  
the privacy of the bidders' input and  
the correctness of the computation

Figure 6. Auction decision cycle

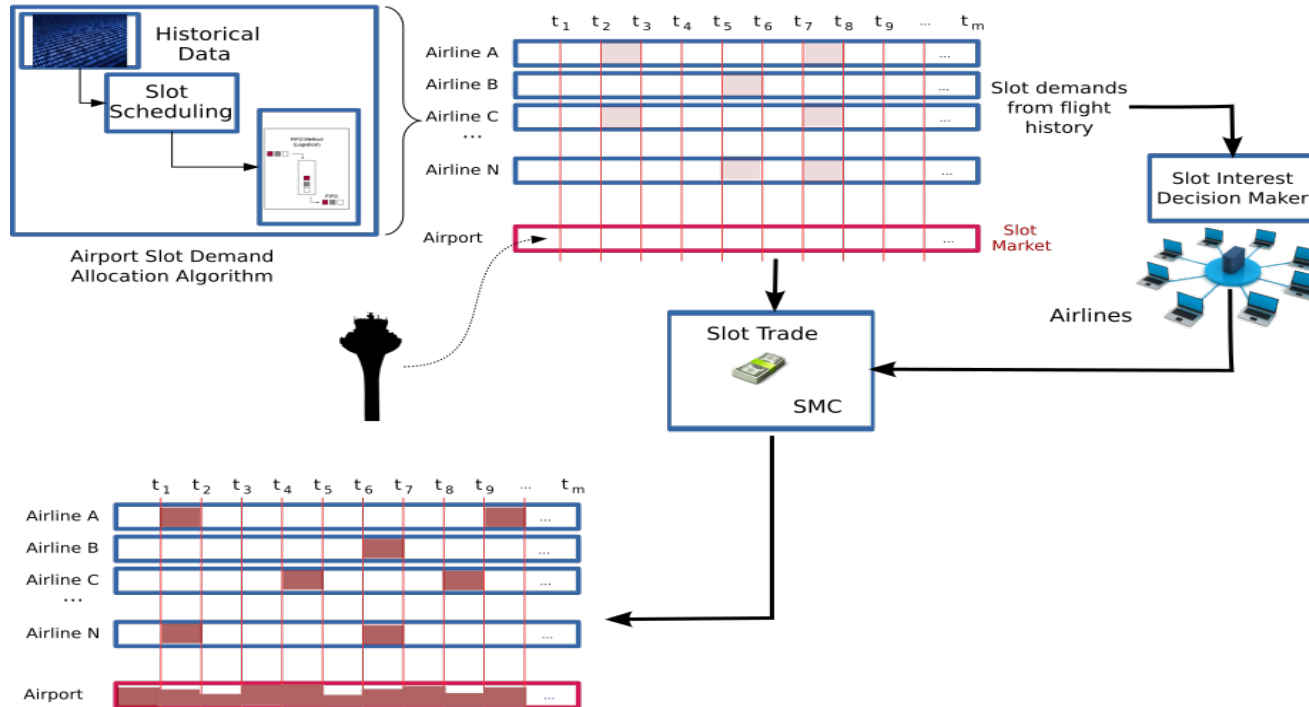
# **Slot Trading & Dynamic Landing Queues**

## **Scenario 1**



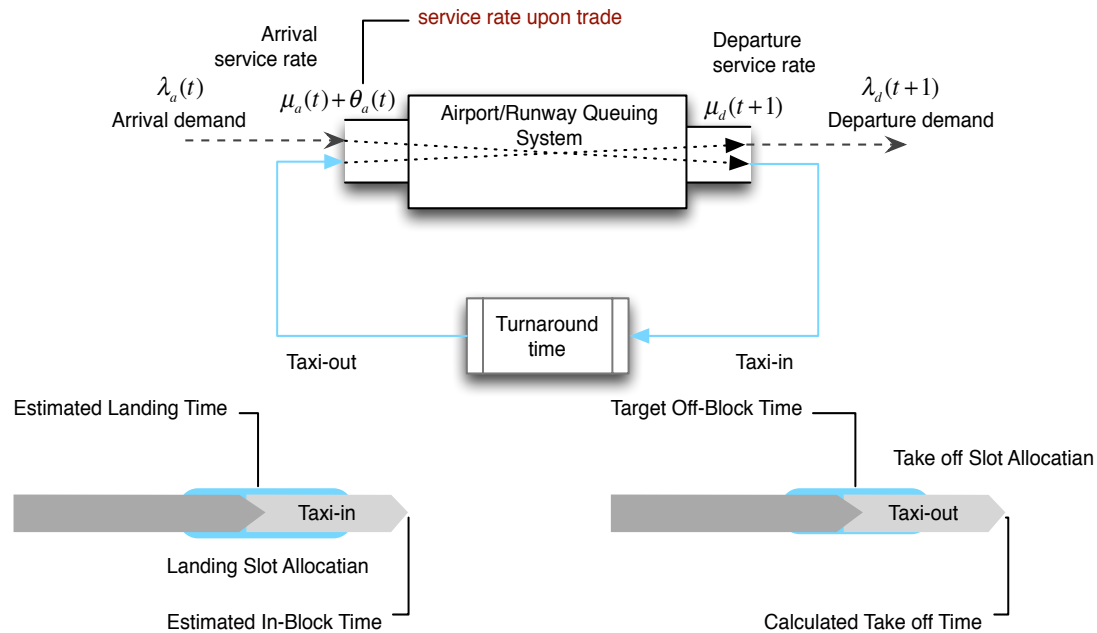
Scenario 1 focuses on initial slot trade from the airports for a long term (6 months before)

## Simulation Model for Scenario #1



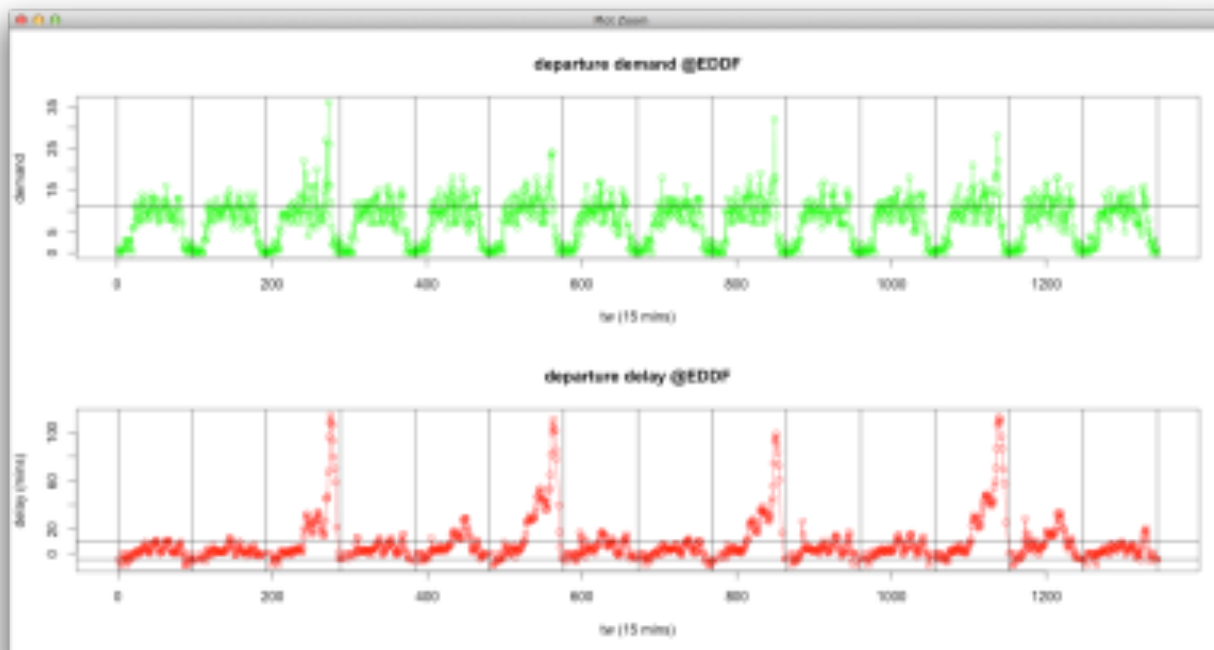
*slot*; is a time interval within which take off has to done such that it is defined between -5 and + 10 minutes from *Calculated Take of Time – CTOT* in Europe (EUROCONTROL 2015).

- Airport Queuing Model



– Static/Dynamics distribution of  $\mu_a(t)$  to demand  $\lambda_a(t)$

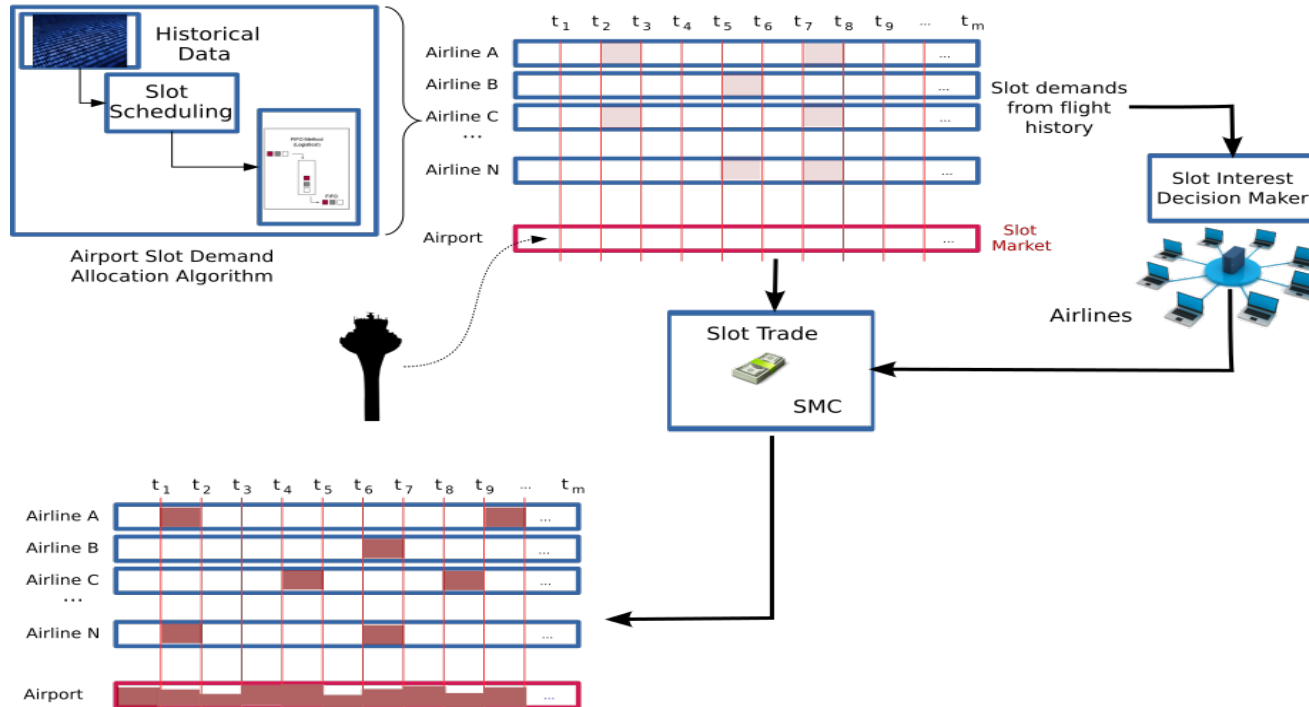
- Fill rates of all available slots vary quite a bit across airports
- Current slot capacities are based on the declared arrival and departure capacities





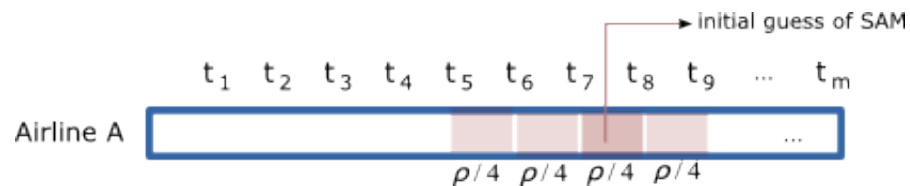
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## Simulation Model for Scenario #1

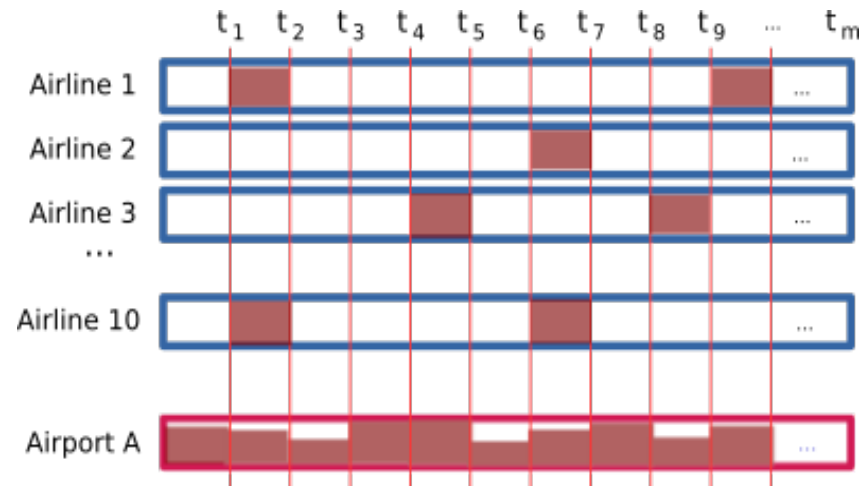


*slot*; is a time interval within which take off has to done such that it is defined between -5 and + 10 minutes from *Calculated Take of Time – CTOT* in Europe (EUROCONTROL 2015).

- *Slot Demand Allocation Model (SAM)* builds schedules for the interest of the airlines.
- Competition begins when at least two airlines want to get same slot exceeding its capacity.



- SMC Engine collects offers.
  - If the result is a tie between two or more participants, the referee provides a notification to the participants and creates a new secure auction.
  - If the minimum price that the seller asks for has not been reached, participants are informed about this.
- Winning price and the winner is disclosed to all participants



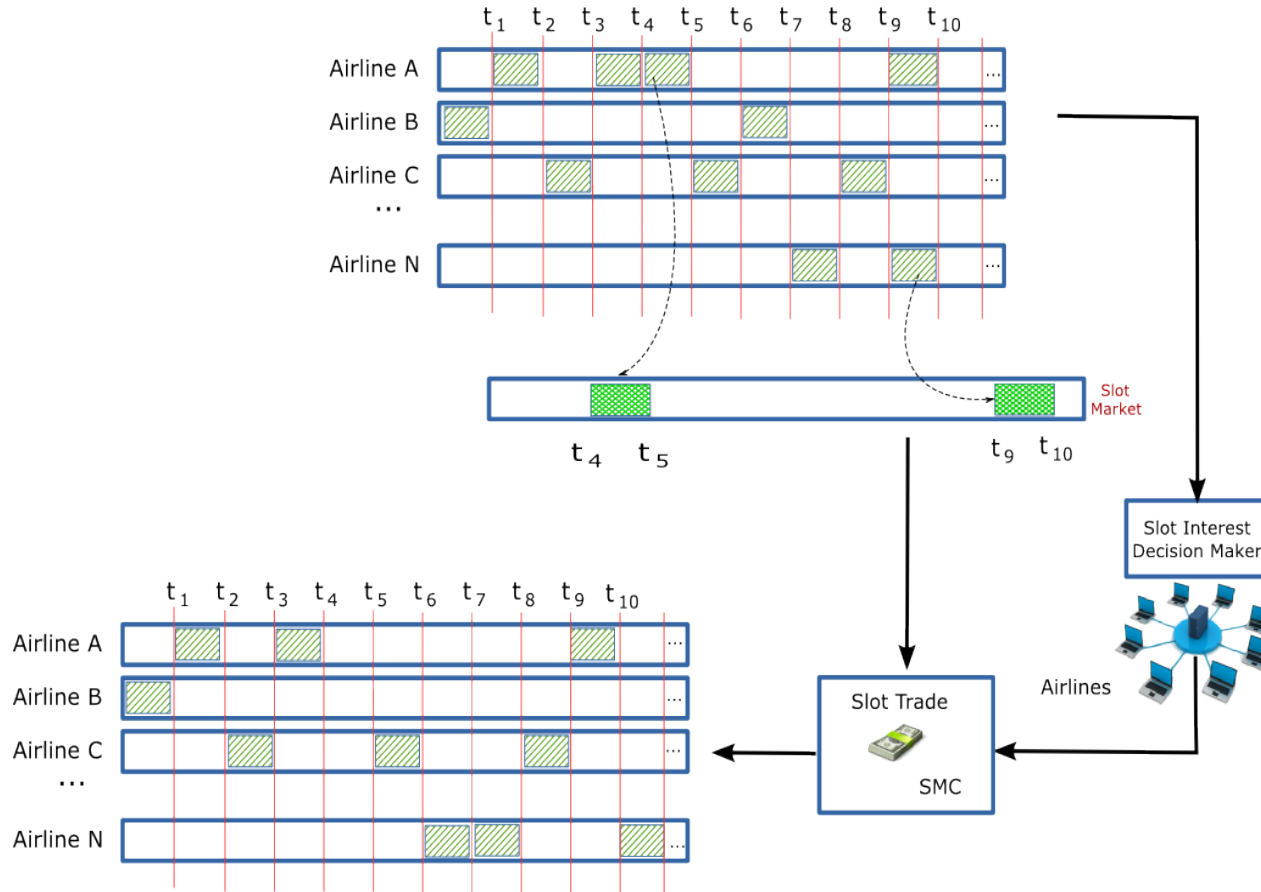
# **Slot Trading & Dynamic Landing Queues**

## **Scenario 2**

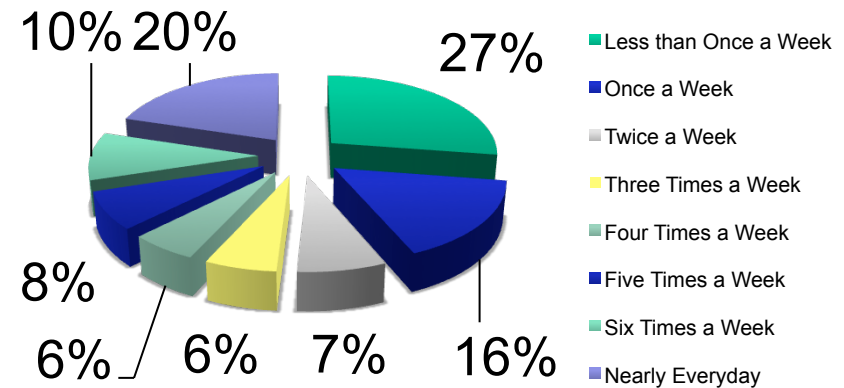
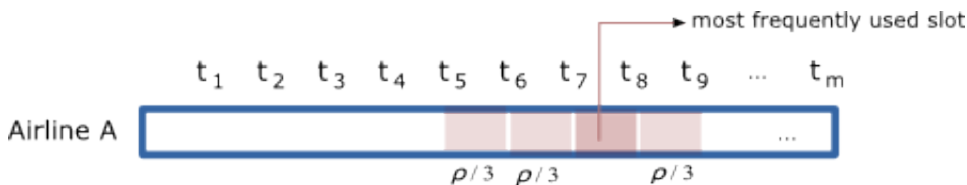


- Scenario 2 focuses on secondary strategic market in which airlines trades their slot between them.

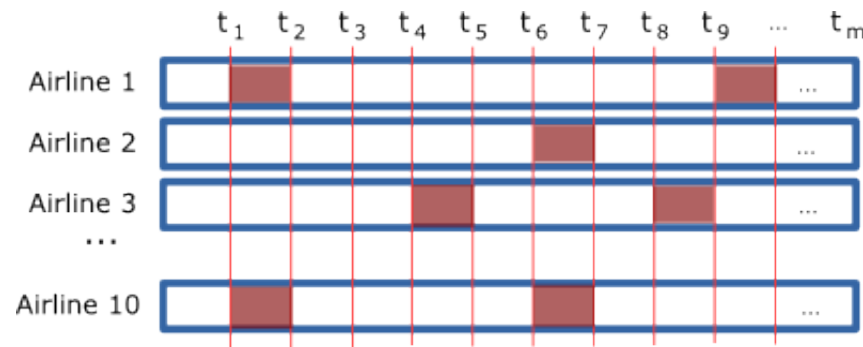
## Simulation Model for Scenario #2



- *Slot Interest Decision Maker (SID)*, hypothetically generates the market and the traders by utilizing flight frequencies
  - The idea behind the concept model is that
    - airlines are interested in selling non-scheduled or least frequently used slots
    - airlines are interested in buying the slots around their most frequently used slots



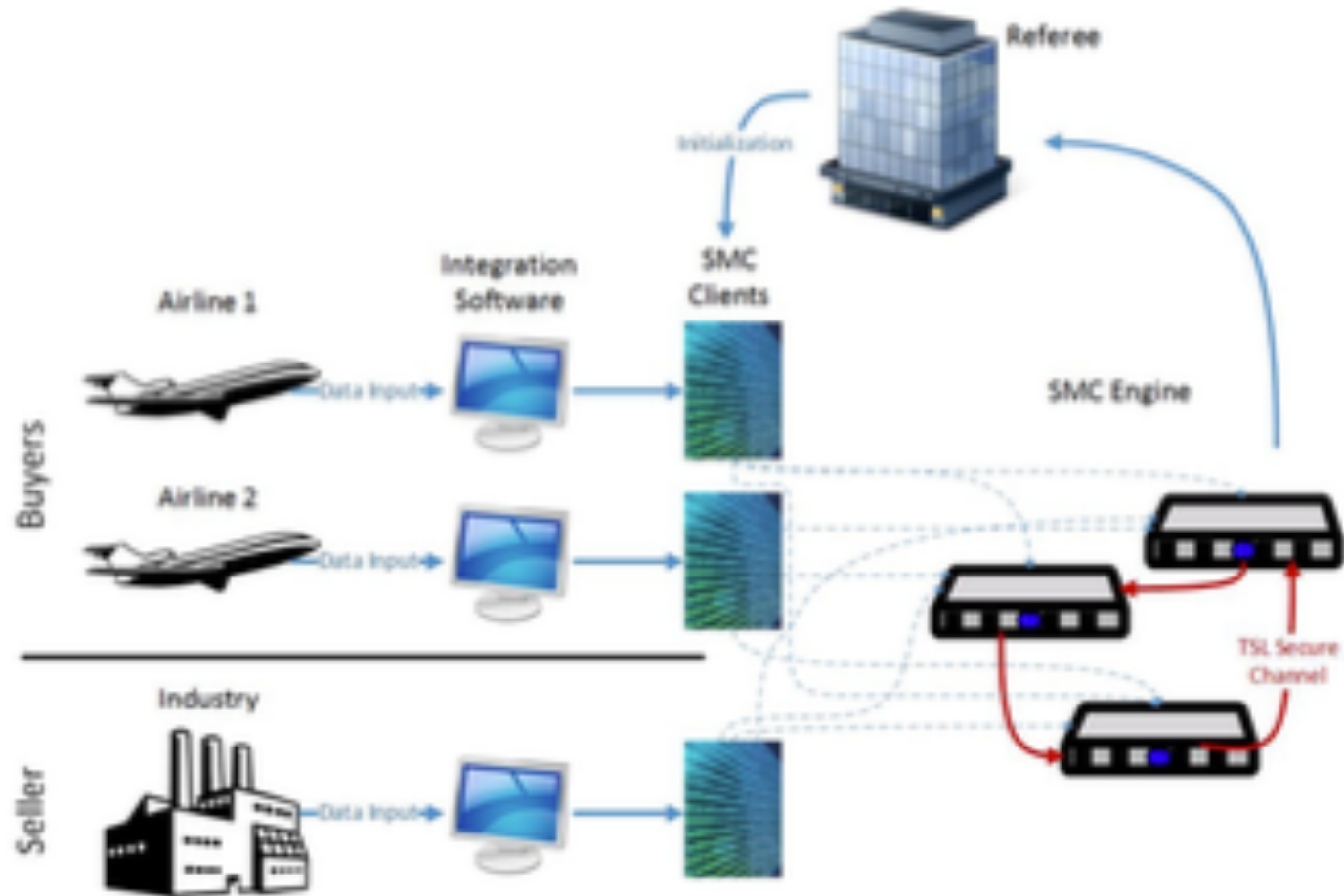
- SMC Engine collects offers.
  - If the result is a tie between two or more participants, the referee provides a notification to the participants and creates a new secure auction.
  - If the minimum price that the seller asks for has not been reached, participants are informed about this.
- Winning price and the winner is disclosed to all participants



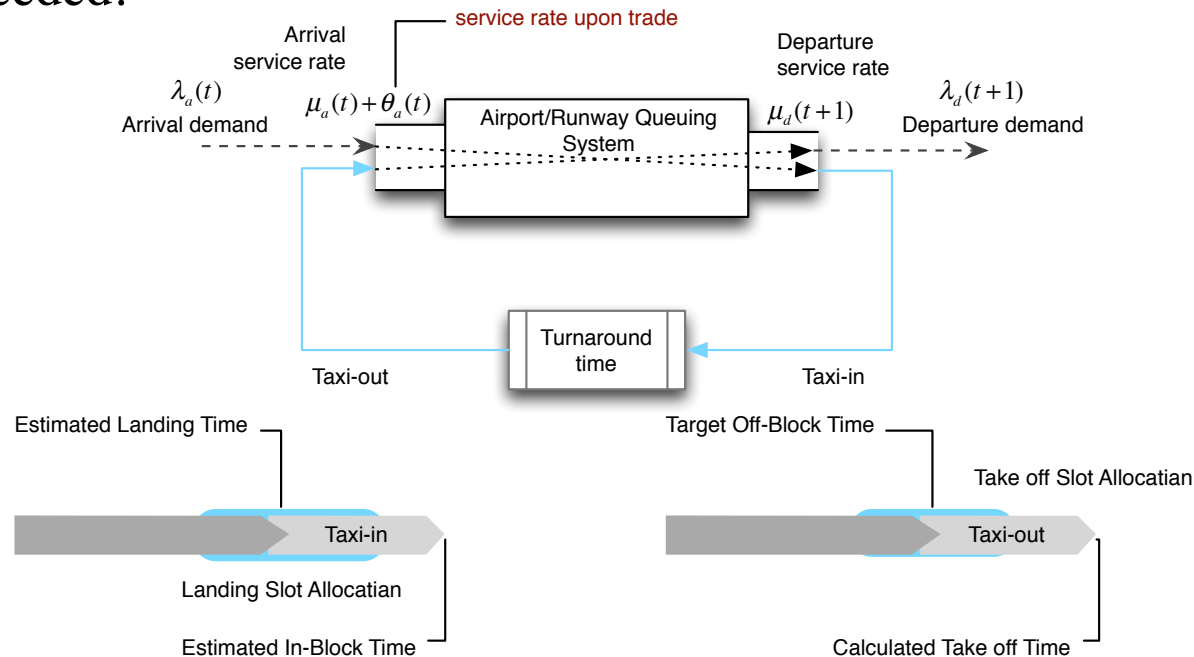


# **Slot Trading & Dynamic Landing Queues**

## **Scenario 3**

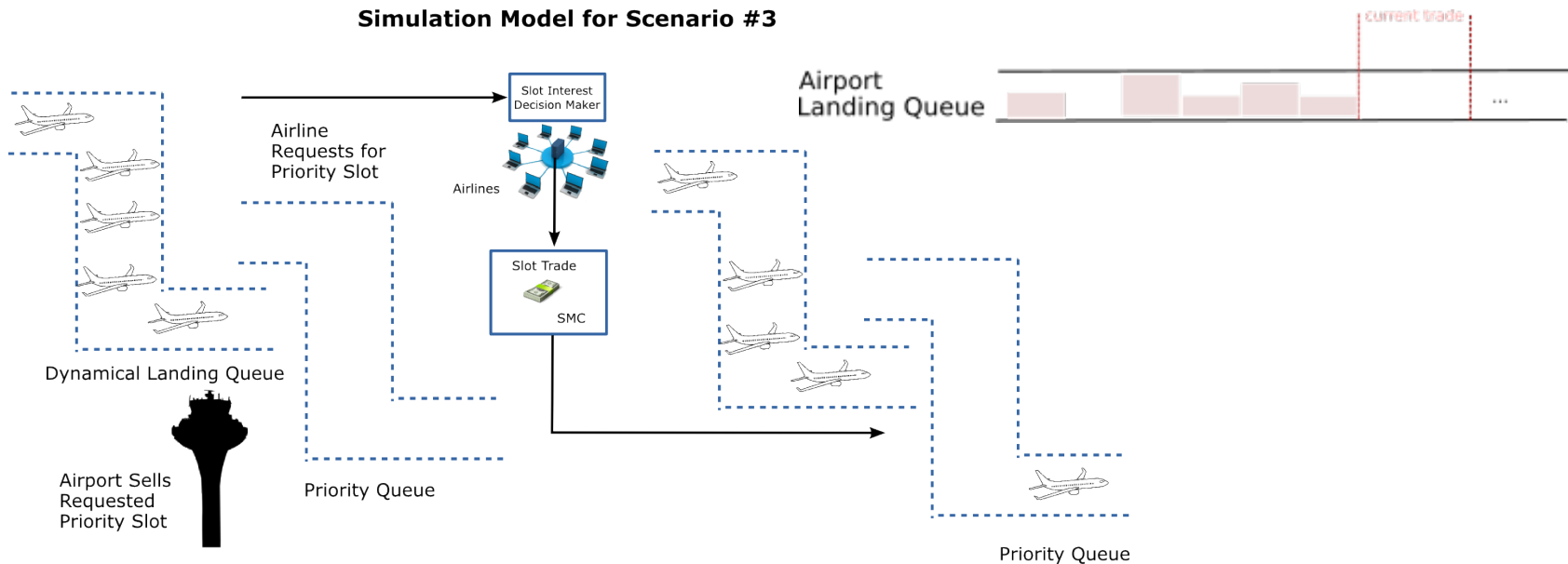


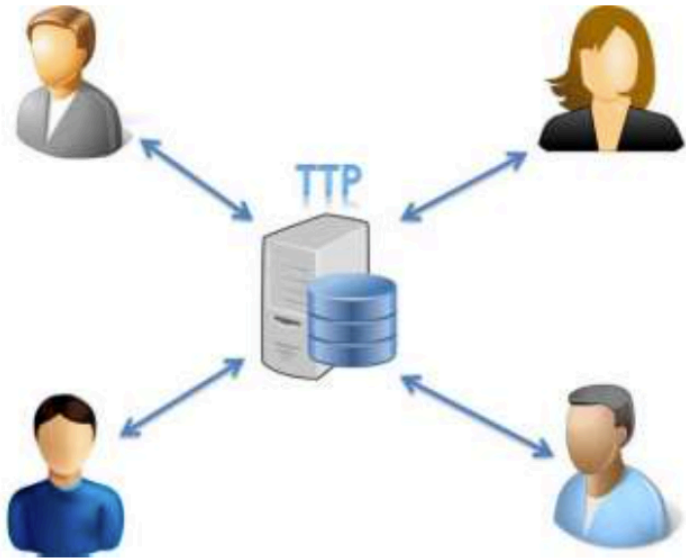
- Scenario 3 focuses on buying a priority landing slot from an airport during approach.
  - Suppose that the airport has an additional runway with capacity  $\theta_a(t)$  which is open to trade
  - This particular runway can be utilized in normal operations, however bid customers can have priority utilizing this capacity as needed.



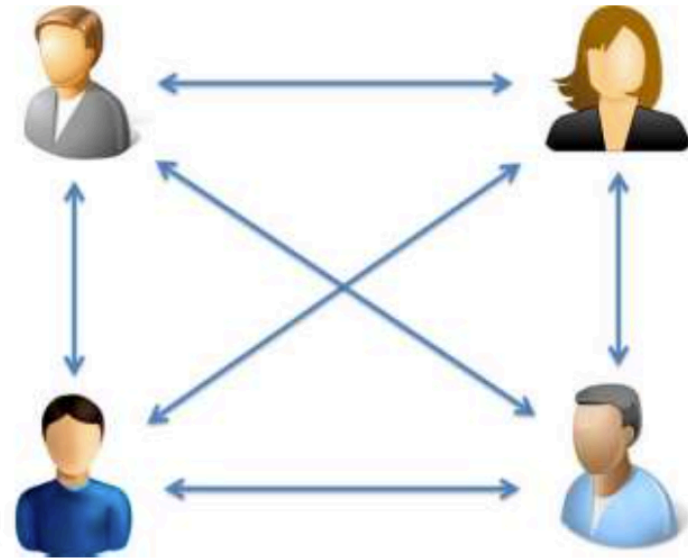
- *Slot Interest Decision Maker (SID)* utilizes current delay
  - Evaluate en-route delays for each landing aircraft.
  - If it is more than 30 minutes, airline is interested in buying a priority slot.

**Simulation Model for Scenario #3**





Trusted Third Party (TTP),  
Traditional Model



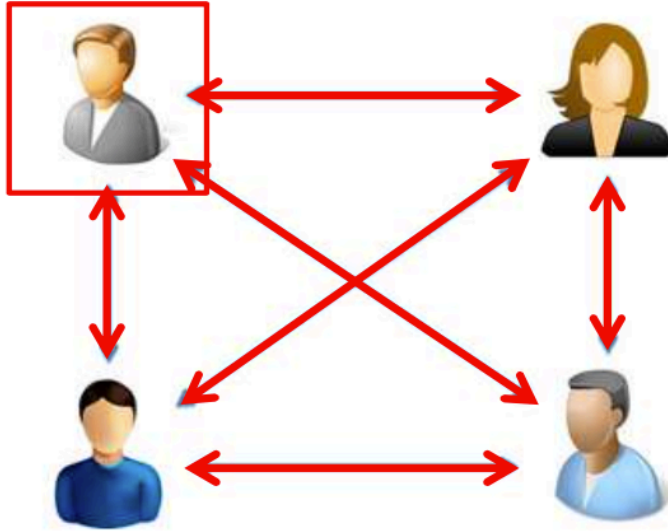
Secure Multiparty Computation  
(SMC)

## Subfield of cryptography

- Term coined by Yao (1982) in the “Millionaire problem”:

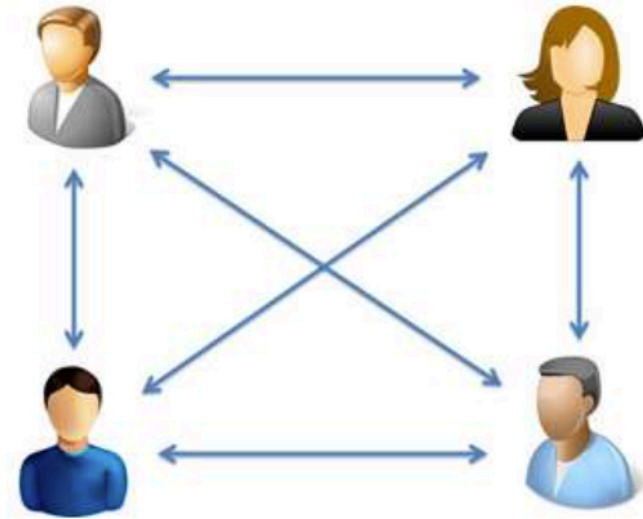
“Two millionaires wish to know who is richer; however, none of them wants the other to find out how much his fortune is worth. How can they know who’s the richest?”

- N players wish to securely compute a given function
  - No one learns anything else than its private input and the result of the computation
- Security ensures:
  - the privacy of the player’s input
  - The correctness of the computation



Party: A participant in the secure computation, also called a player.

Protocol: In general terms, it describes how the algorithms should be used, how the players interact.



**Passive  
Adversary**

Semi-honest party (honest but curious party):

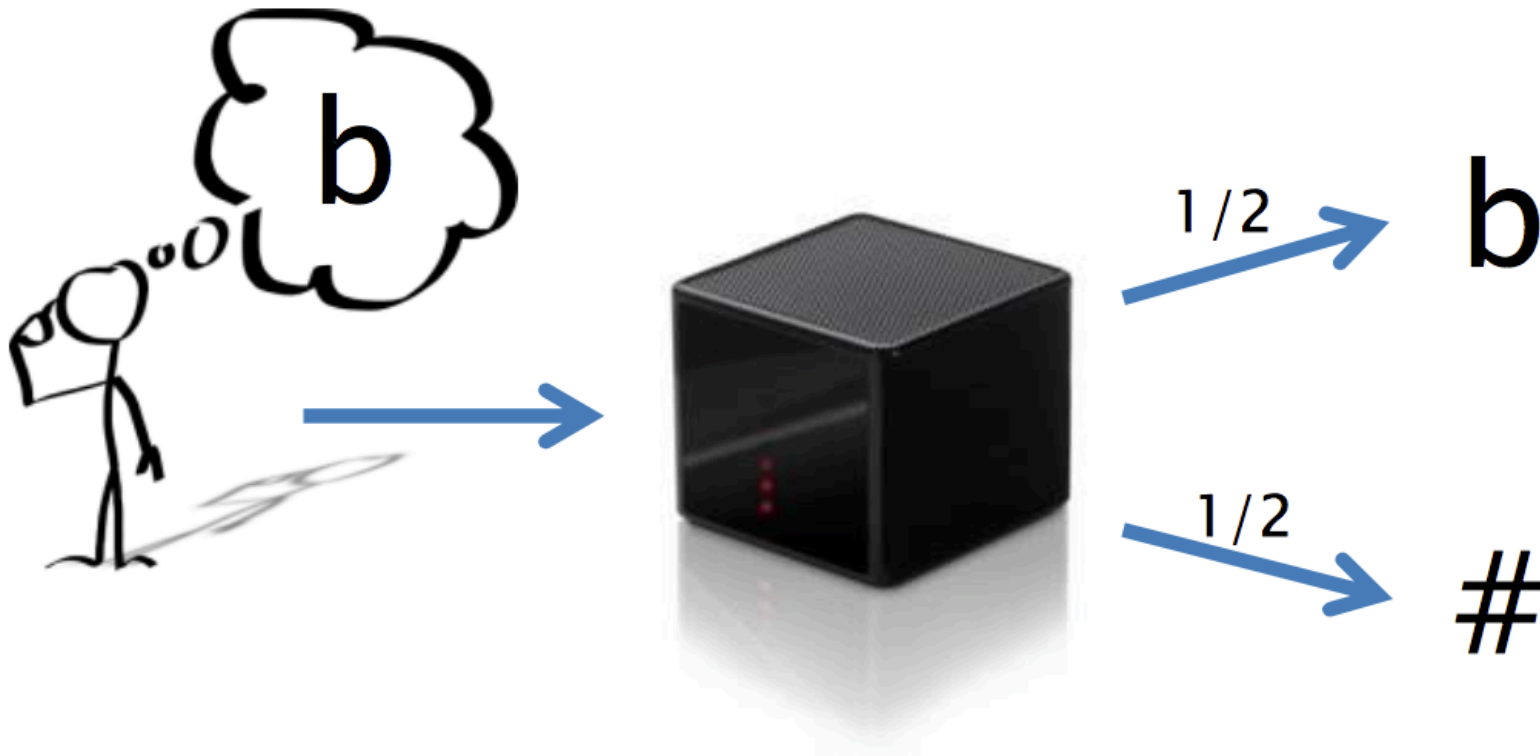
- parties in the computation are corrupted by a passive adversary
- parties will always follow the protocol correctly
- parties will try to learn the others private data by examining all the data they get
- the outcome of the computation won't be affected



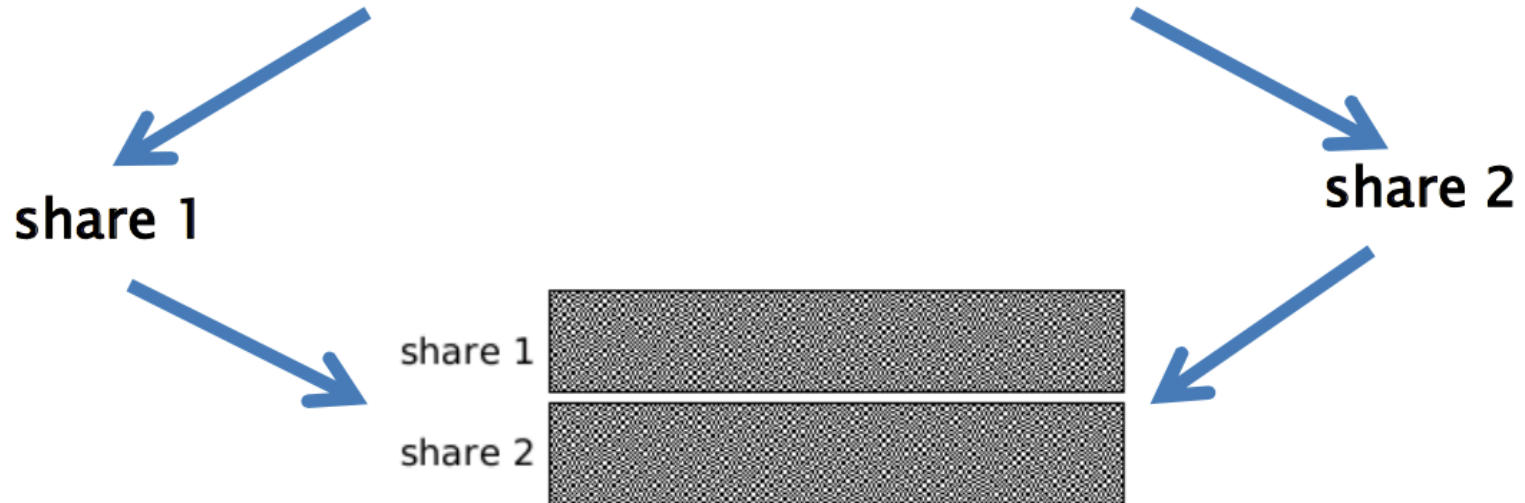
Primitive	Remarks	Usage
Oblivious Transfer (OT)	<ul style="list-style-type: none"> <li>• Sends data with a <math>\frac{1}{2}</math> probability of delivery</li> <li>• Used as an arithmetic black box</li> </ul>	Usually used in two-party computations
Secret Sharing (SS)	<ul style="list-style-type: none"> <li>• Split the private data into shares</li> <li>• Unbreakable without the needed number of shares</li> </ul>	Most widely used primitive in the construction of SMC protocols
Homomorphic Encryption (HE)	<ul style="list-style-type: none"> <li>• Doesn't need to generate shares, it can perform the computation over the encrypted data directly</li> <li>• Very powerful, but complex to implement</li> </ul>	Theoretical approach, too costly and complex to implement

Rabin's oblivious transfer is kind of formalization of "noisy wire" communication

- Sender sends bit  $b$  into OT machine
- Machine then flips the coin, and with probability  $1/2$  sends  $b$  to receiver.
- Sender does not know which output receiver received



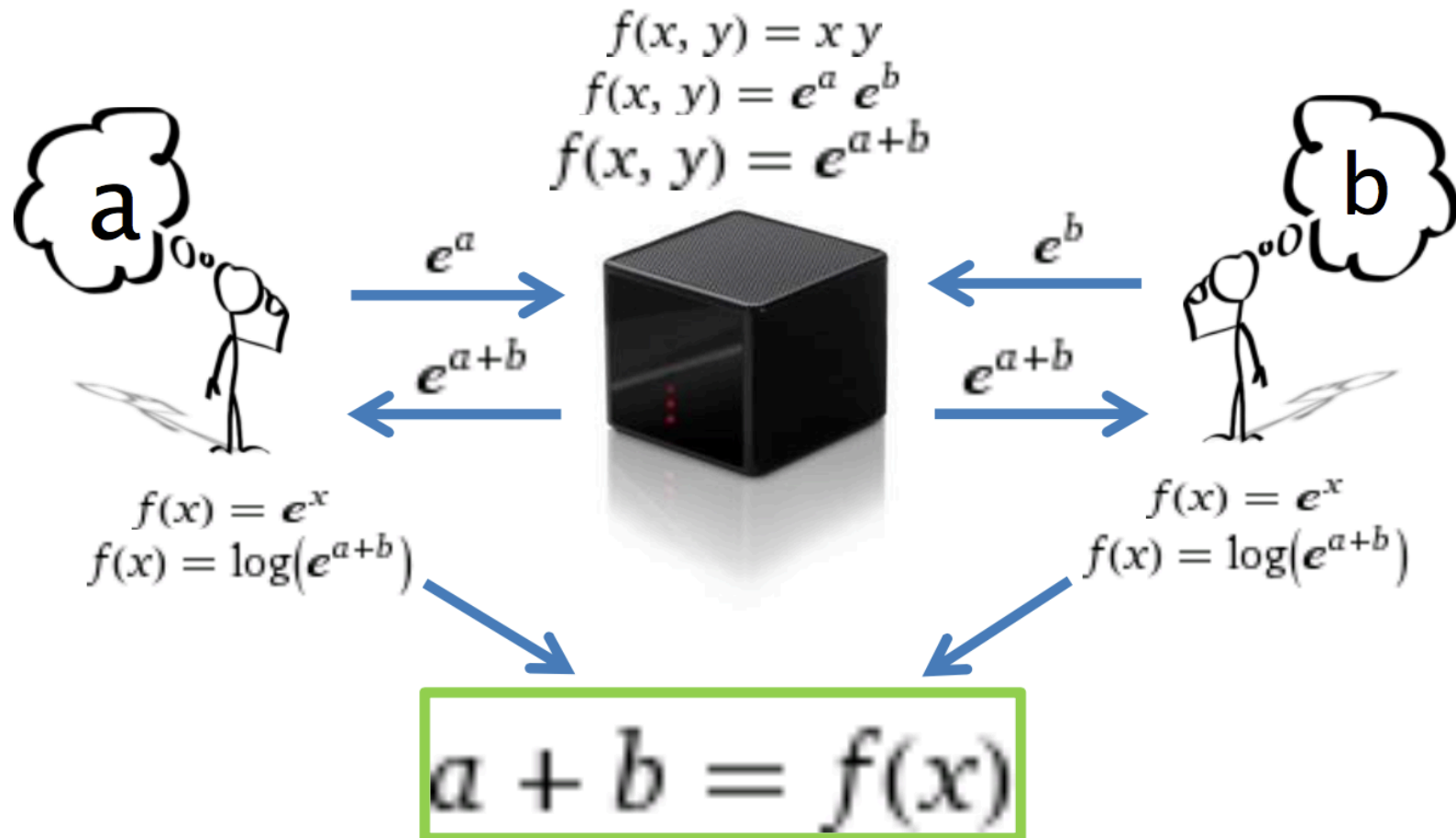
# WIKIPEDIA

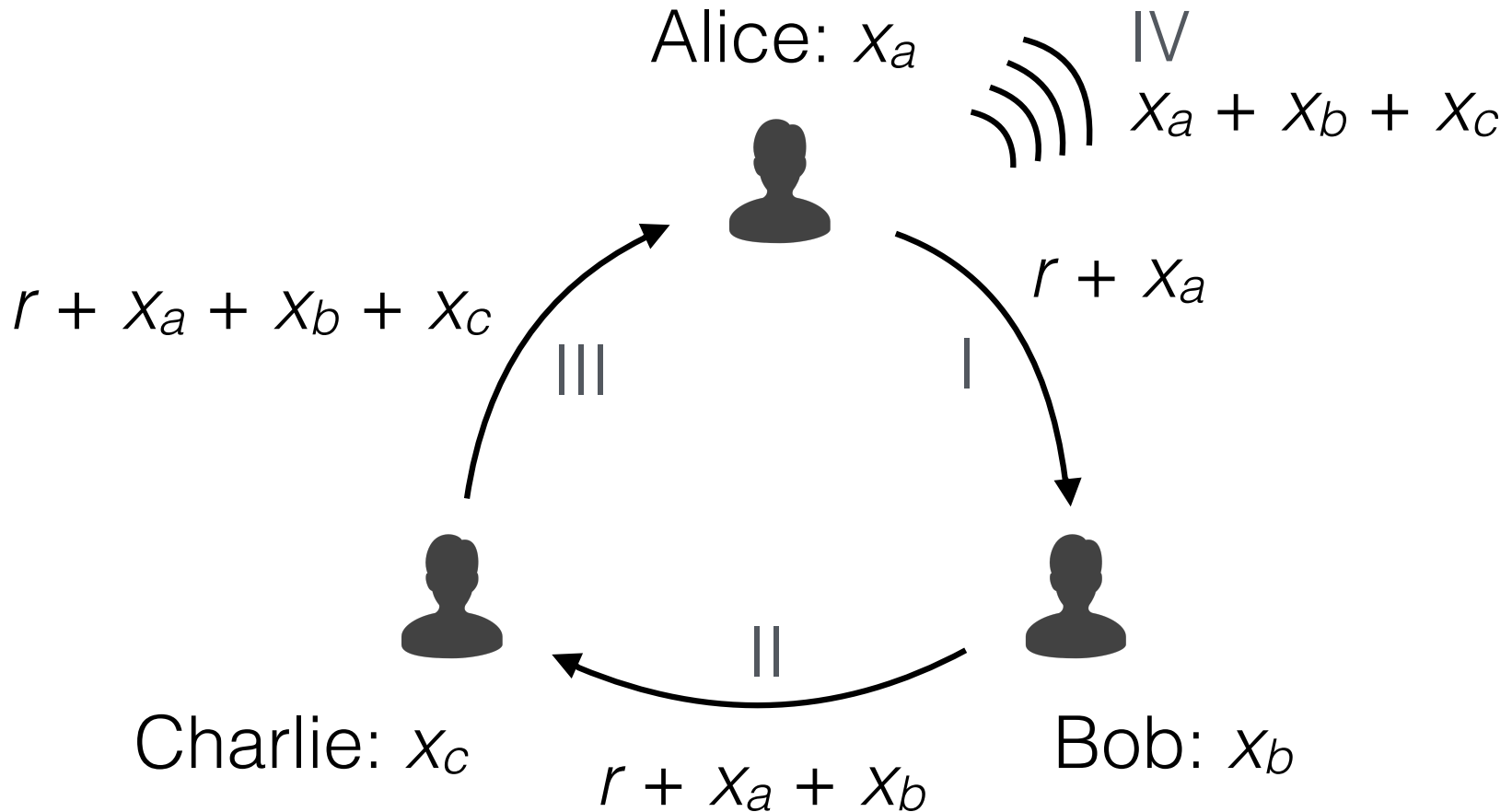




Let's calculate  $a + b$ !

$$\exp(x + y) = (\exp x)(\exp y)$$

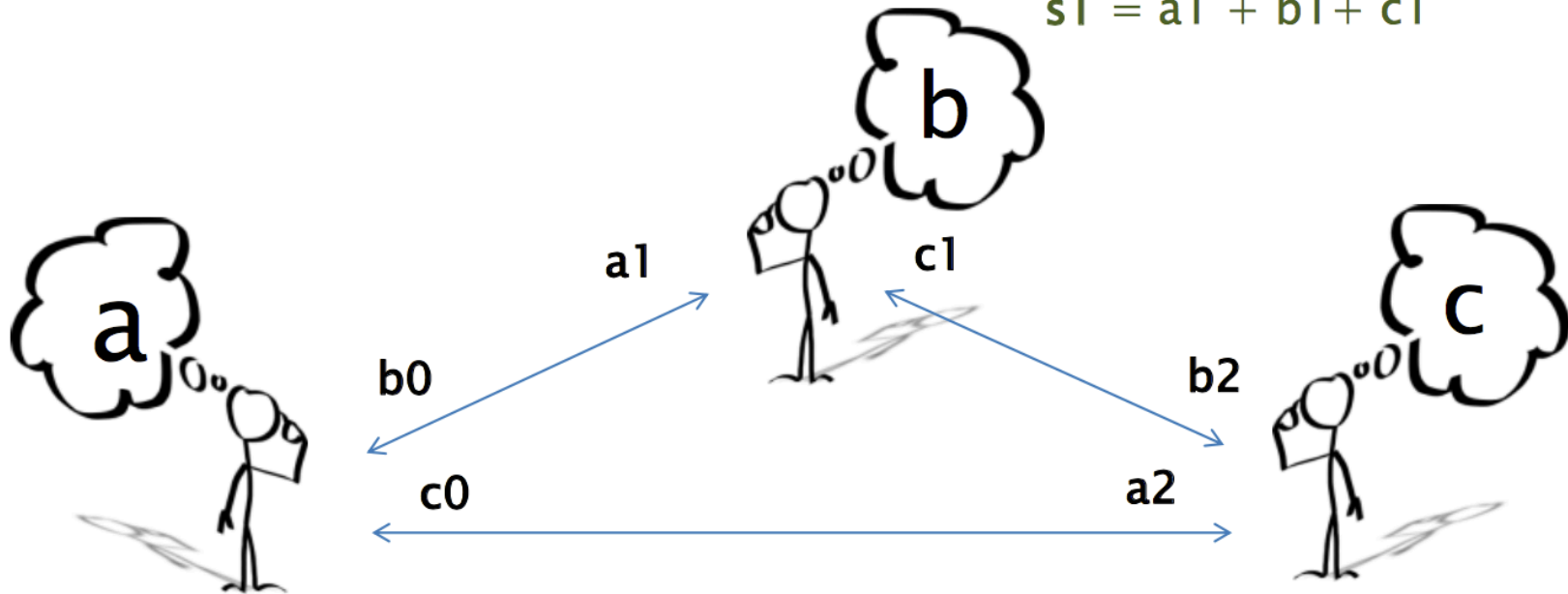




Let's *securely* calculate  $a + b + c$ !

$$b = b_0 + b_1 + b_2$$

$$s_1 = a_1 + b_1 + c_1$$



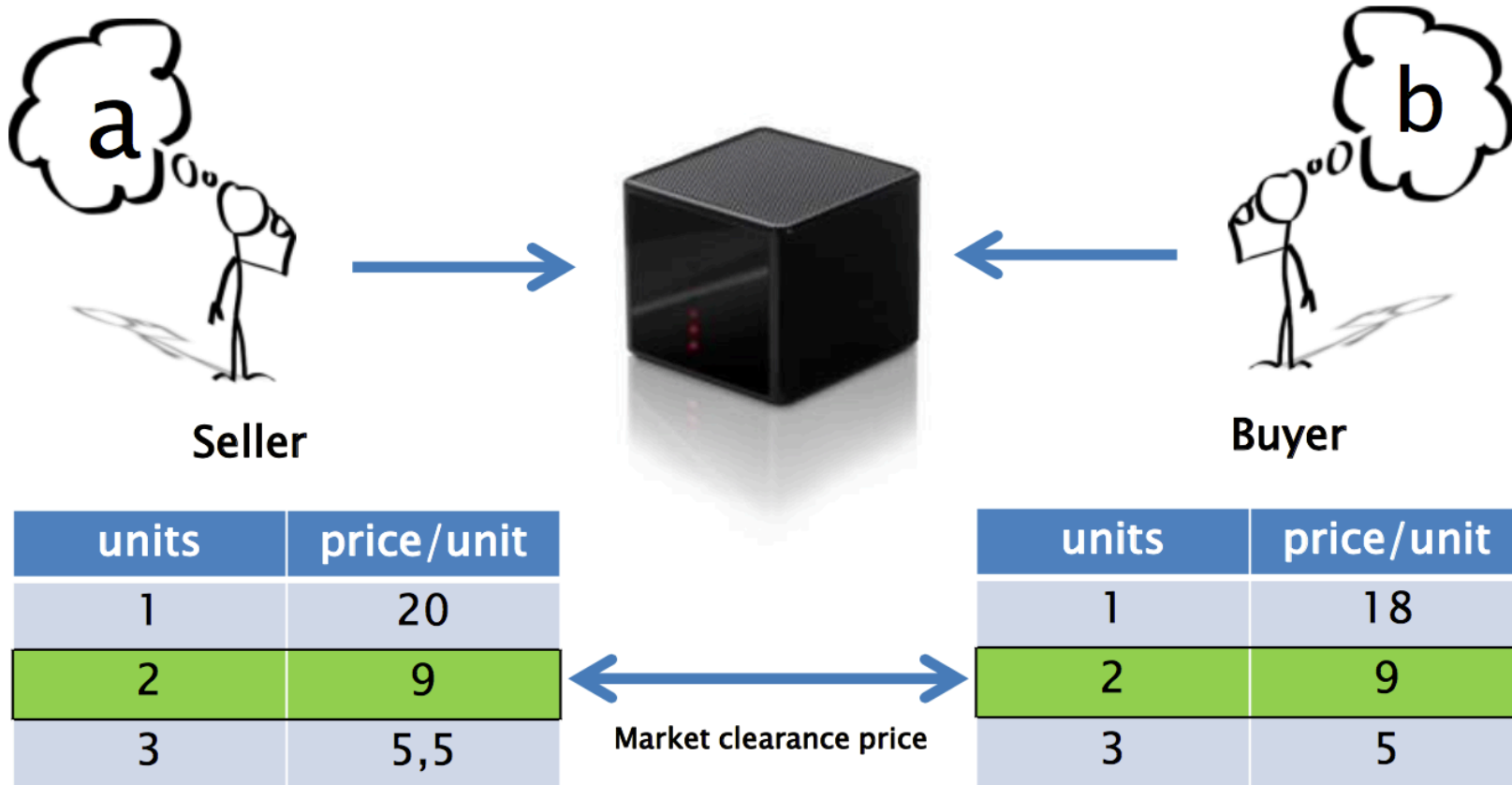
$$a = a_0 + a_1 + a_2$$

$$s_0 = a_0 + b_0 + c_0$$

$$c = c_0 + c_1 + c_2$$

$$s_2 = a_2 + b_2 + c_2$$

$$s_0 + s_1 + s_2 = a + b + c$$







**Company1**



**Company 2**



## **Sector benchmarking:**

- Statistical Data
- Strategic Ranking
- Anonymity